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# Thermodynamic properties of $\text{SmMnO}_3$ , $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$ and $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$

Renu Choithrani<sup>1</sup>, N K Gaur<sup>1</sup> and R K Singh<sup>2</sup>

<sup>1</sup> Department of Physics, Barkatullah University, Bhopal (MP) 462026, India

<sup>2</sup> School of Basic Sciences, MATS University, Raipur (CG) 492002, India

E-mail: [renuchoithrani@gmail.com](mailto:renuchoithrani@gmail.com)

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## Abstract

We have investigated thermodynamic properties of the perovskite  $\text{Sm}(\text{Ca}, \text{Sr})\text{MnO}_3$  manganites, probably for the first time, using the rigid ion model (RIM) after modifying its framework to incorporate the van der Waals attraction and the short-range Hafemeister–Flygare type overlap repulsion operating between the first and second neighbour ions. We have found that the evaluated thermodynamic properties reproduce the corresponding experimental data well, implying that the modified RIM properly represents the elastic nature of these perovskite manganite systems. The results of the present investigation can be further improved by including the ferromagnetic spin wave contribution and Jahn–Teller distortion effect in the framework of the modified RIM.

## 1. Introduction

During the past few decades, the effects of strongly correlated electrons and/or charge ordered (CO) phenomena have appeared in some major developments beginning with the mechanism of high  $T_c$  superconductivity [1] in cuprates followed (a decade later) by the observation of colossal magnetoresistance (CMR) [2] in perovskite manganites [3–5]. These manganites exhibit a rich phase diagram including different types of ordering phenomena and ground states, such as charge order, orbital order, and antiferromagnetic (AFM) or ferromagnetic (FM) insulators or metals [6, 7]. The CMR phenomena has mostly been found and studied in the perovskite manganites with the general formula  $\text{RE}_{1-x}\text{AE}_x\text{MnO}_3$  (where  $\text{RE} = \text{La}, \text{Pr}, \text{Nd}, \text{Sm}, \text{Eu}, \text{Gd}, \text{Ho}, \text{Tb}, \text{Y}$  etc and  $\text{AE} = \text{Sr}, \text{Ca}, \text{Ba}, \text{Pb}$ ). In the present investigation, we have focused our attention on the pure  $\text{SmMnO}_3$  and the electron-doped  $\text{Sm}_{1-x}\text{Sr}_x\text{MnO}_3$  ( $x = 0.45$ ) and  $\text{Ca}_{1-x}\text{Sm}_x\text{MnO}_3$  ( $x = 0.15$ ) manganites. These manganites exhibit several interesting and anomalous features due to the competition among the electronic phases, ferromagnetic metallic (FM) state and charge-orbital-ordered (CO/OO) states with the collectively Jahn–Teller coupled lattice deformations (as reviewed in detail by Tokura [4]).

The crystal structure of  $\text{SmMnO}_3$  (space group  $pnma$ ) has an orthorhombic perovskite structure [8] with four formula units per unit cell and four 3d electrons: three  $t_{2g}$  and one  $e_g$

electrons [7]. Since three  $t_{2g}$  electrons form an orbitally closed shell, many physical properties are believed to be governed by its  $e_g$  electrons. The occurrence of the spin and orbital ordered state has been understood in terms of the cooperative Jahn–Teller (JT) distortion [9]. The pure  $\text{SmMnO}_3$  exhibits a Jahn–Teller distorted orthorhombic structure and shows a sharp peak in the specific heat at  $\sim 59$  K due to the A-type AF ordering [10] and this feature is remarkable in the experimental specific heat.

The phase diagram of  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  shows two critical end points in zero magnetic field (128.6 and 113.3 K) [11]. The crystal structure of  $\text{Sm}_{0.55}\text{Sr}_{0.15}\text{MnO}_3$  is orthorhombic perovskite as determined from XRD data by Abdulvagidor *et al* [11]. The  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  manganite has been found to exhibit some unique properties, such as the structural transformation from an orthorhombic  $Pnma$  phase to a monoclinic  $P2_1/m$  phase [12] on lowering the temperature to 115 K [13]. Also, the low-temperature phase of  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  is a C-type antiferromagnet, which possesses, however, a weak ferromagnetic moment [13]. The temperature dependence of the specific heat of  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  reveals one well-pronounced anomaly at  $T \sim 115$  K [12–14].

The study of pure  $\text{SmMnO}_3$  and doped  $\text{Sm}(\text{Ca}, \text{Sr})\text{MnO}_3$  perovskite manganites is motivated by their interesting features of the CMR effect, antiferromagnetic (low temperature) ground state and strong Jahn Teller distortion. There is much experimental evidence indicating the importance of the

electron–lattice coupling in manganese oxides [15–17] from which one can see that there is a close relation between the lattice dynamics and the electronic and magnetic properties. These features indicate the necessity of understanding the interaction mechanism and physical properties of these manganites.

Recently, we have successfully shown the thermodynamic behaviour of some manganites [18–20], by using a modified rigid ion model (MRIM) [18–20]. The major contribution to the pair potential of MRIM is contributed by the long-range (LR) Coulomb attraction, which is counterbalanced by the short-range (SR) overlap repulsion having their origin in the Pauli exclusion principle. This SR interaction is expressed by a Hafemeister–Flygare (HF) [21] type overlap repulsion effective up to the second neighbour ions. This potential also incorporates the effects of the van der Waals (vdW) attraction (Tosi and Fumi [22]) arising from the dipole–dipole (d–d) and dipole–quadrupole (d–q) interactions, whose coefficients are estimated from the Slater–Kirkwood variational (SKV) [23] approach, which treats both the ions (cations and anions) as polarizable. Motivated from such a realistic and qualitative representation of the interionic potential and its versatile applicability to describing the cohesive and physical properties of solids and alloys (Singh [24] and Varshney *et al* [25]), we thought it pertinent to apply this MRIM, probably for the first time, to explore the thermodynamic properties of  $\text{SmMnO}_3$ ,  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  and  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$ , as very scant attention has been paid on them by theoretical investigators. The interaction potential of the MRIM is described in section 2. The computed results are presented and discussed in section 3.

## 2. Essential formalism of MRIM

We have formulated the modified rigid ion model (MRIM) [18–20] by incorporating the effects of the long-range (LR) Coulomb attraction, the short-range (SR) Hafemeister–Flygare (HF) [21] type overlap repulsion effective up to the second neighbour ions and the van der Waals (vdW) attraction due to the dipole–dipole (d–d) and dipole–quadrupole (d–q) interactions in the framework of the RIM [24, 26]. The total cohesive energy ( $\phi$ ) of the MRIM is expressed as [18–20]:

$$\begin{aligned} \phi = & -\frac{e^2}{2} \sum_{kk'} Z_k Z_{k'} r_{kk'}^{-1} + \left[ nb_1 \beta_{kk'} \exp\{(r_k + r_{k'} - r_{kk'})/\rho_1\} \right. \\ & + \frac{n'}{2} b_2 [\beta_{kk} \exp\{(2r_k - r_{kk})/\rho_2\} + \beta_{k'k'} \exp\{(2r_{k'} \\ & \left. - r_{k'k'})/\rho_2\}] - \sum_{kk'} c_{kk'} r_{kk'}^{-6} - \sum_{kk'} d_{kk'} r_{kk'}^{-8}. \end{aligned} \quad (1)$$

Here,  $k(k')$  denote the type of  $k(k')$  ions. In the orthorhombic perovskite structure,  $k$  represents cations (A, B) and  $k'$  denotes the type of ( $\text{O}_1$ ,  $\text{O}_2$ ) ions with general formula  $\text{ABO}_3$  (such as  $\text{SmMnO}_3$ ). The summation in the first, fourth and fifth terms in equation (1) is performed over all the  $kk'$  ions. The second and third terms represent the short-range HF type overlap repulsion expressed as an exponential function of the separations  $(r_k + r_{k'} - r_{kk'})$ ,  $(2r_k - r_{kk})$  and  $(2r_{k'} - r_{k'k'})$ . The

symbols  $Z_k (Z_{k'})$  and  $r_k (r_{k'})$  are the ionic charges and radii of the  $k(k')$  ions.  $n(n')$  represent the number of the first (second) neighbour ions.  $\beta_{kk'}$  are the Pauling coefficients [27]:

$$\beta_{kk'} = 1 + (z_k/n_k) + (z_{k'}/n_{k'}) \quad (2)$$

with  $z_k (z_{k'})$  and  $n_k (n_{k'})$  as the valence and number of electrons in the outermost orbit of  $k(k')$  ions. In equation (1),  $r_{kk'}$  and  $r_{kk} (=r_{k'k'})$  are, respectively, the first and second neighbour separations and their values are obtained for Sm substitutions ( $x$ ) using the well known Vegard's law [28].

In equation (1), the first term represents the long-range Coulomb attraction, the second and third terms are the short-range HF [21] type overlap repulsion and the fourth and fifth terms are the vdW attraction energies due to d–d and d–q interactions, whose significance has been shown from the qualitative and quantitative analysis for some other systems of solids by Tosi and others [22]. The symbols  $c_{kk'}$  and  $d_{kk'}$  are the corresponding vdW coefficients, whose values are determined by using their expressions [18–20] derived from the Slater–Kirkwood variational (SKV) [23] method and by treating both the cations and anions as polarizable:

$$c_{kk'} = (3e\hbar\alpha_k\alpha_{k'}/2m)[(\alpha_k/N_k)^{1/2} + (\alpha_{k'}/N_{k'})^{1/2}]^{-1} \quad (3)$$

$$\begin{aligned} d_{kk'} = & (27e\hbar^2\alpha_k\alpha_{k'}/8m)[(\alpha_k/N_k)^{1/2} + (\alpha_{k'}/N_{k'})^{1/2}]^2 \\ & \times [(\alpha_k/N_k)^{1/2} + \frac{20}{3}(\alpha_k\alpha_{k'}/N_k N_{k'})^{1/2}]^{-1} \end{aligned} \quad (4)$$

where  $m$  and  $e$  are the mass and charge of electron, respectively.  $\alpha_k (\alpha_{k'})$  are the electronic polarizabilities of  $k(k')$  ions;  $N_k (N_{k'})$  are the effective number of electrons responsible for the polarization of  $k(k')$  ions. The values of  $c_{kk'}$  and  $d_{kk'}$  are evaluated using the equations (3) and (4) and following the procedure adopted in our recent papers [19, 20].

The model parameters (hardness ( $b$ ) and range ( $\rho$ )) are determined from the equilibrium condition:

$$[d\phi(r)/dr]_{r=r_0} = 0 \quad (5)$$

and the bulk modulus:

$$B = (9Kr_0)^{-1} [d^2\phi(r)/dr^2]_{r=r_0}. \quad (6)$$

Here,  $r_0$  and  $r$  are the interionic separations in the equilibrium and otherwise states of the system, respectively. The symbol  $K$  is the crystal structure constant.

The values of the input data ( $r_0$ ,  $B$ ) for the evaluation of the four disposable model parameters ( $b_1$ ,  $\rho_1$ ) and ( $b_2$ ,  $\rho_2$ ) corresponding to the ionic bonds Mn–O and Sm/Sr or Ca–O for different compositions ( $x = 0.45$  and  $0.15$ ) and temperatures  $15 \text{ K} \leq T \leq 300 \text{ K}$  [19] have been obtained from the well known Vegard's law using their experiment data from [10–12, 29–32]. The vdW coefficients  $c_{kk'}$  and  $d_{kk'}$  are evaluated from the SKV [23] method for the present manganites. The values of these model parameters ( $b_1$ ,  $\rho_1$ ) and ( $b_2$ ,  $\rho_2$ ) are depicted in tables 1–3 for  $\text{SmMnO}_3$ ,  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  and  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  perovskites, respectively, and used to describe various physical properties of the present system of pure and doped manganites.

**Table 1.** Model parameters and thermodynamic properties of SmMnO<sub>3</sub>.

| <i>T</i> (K) | Model parameters     |                                       |                      |                                       | Thermodynamic properties |  |   |                     |                    |                    |
|--------------|----------------------|---------------------------------------|----------------------|---------------------------------------|--------------------------|--|---|---------------------|--------------------|--------------------|
|              | Mn–O<br>$\rho_1$ (Å) | Mn–O $b_1$<br>(10 <sup>-12</sup> erg) | Sm–O<br>$\rho_2$ (Å) | Sm–O $b_2$<br>(10 <sup>-12</sup> erg) | $\phi$<br>(eV)           | $f$<br>(10 <sup>4</sup> dyn cm <sup>-1</sup> ) | $\beta$<br>(10 <sup>-12</sup> dyn <sup>-1</sup> cm <sup>2</sup> ) | $\nu_0$<br>(THz)    | $\theta_D$<br>(K)  | $\gamma$           |
| 15           | 0.616                | 1.868                                 | 0.804                | 2.121                                 | -143.631                 | 11.98  | 3.067   | 9.125               | 437.97             | 2.09               |
| 60           | 0.615                | 1.862                                 | 0.803                | 2.117                                 | -143.671                 | 12.03  | 3.057   | 9.141               | 438.74             | 2.09               |
| 105          | 0.614                | 1.856                                 | 0.801                | 2.114                                 | -143.712                 | 12.07  | 3.048   | 9.157               | 439.51             | 2.10               |
| 195          | 0.612                | 1.845                                 | 0.799                | 2.106                                 | -143.792                 | 12.15  | 3.029   | 9.189               | 441.04             | 2.12               |
| 240          | 0.611                | 1.839                                 | 0.798                | 2.103                                 | -143.832                 | 12.20  | 3.019   | 9.205               | 441.80             | 2.13               |
| 300          | 0.610                | 1.831                                 | 0.796                | 2.098                                 | -143.885                 | 12.25  | 3.007   | 9.226               | 442.82             | 2.14               |
| (Expt)       | —                    | —                                     | —                    | —                                     | (-140.52) <sup>a</sup>   | —  | —   | (8.58) <sup>b</sup> | (465) <sup>c</sup> | (2-3) <sup>d</sup> |

<sup>a</sup> Reference [33]; <sup>b</sup> reference [34]; <sup>c</sup> reference [10]; <sup>d</sup> reference [35].

**Table 2.** Model parameters and thermodynamic properties of Sm<sub>0.55</sub>Sr<sub>0.45</sub>MnO<sub>3</sub>.

| <i>T</i> (K) | Model parameters     |                                       |                         |  | Thermodynamic properties |  |   |                     |                   |                    |
|--------------|----------------------|---------------------------------------|-------------------------|--|--------------------------|--|---|---------------------|-------------------|--------------------|
|              | Mn–O<br>$\rho_1$ (Å) | Mn–O $b_1$<br>(10 <sup>-12</sup> erg) | Sm/Sr–O<br>$\rho_2$ (Å) | Sm/Sr–O $b_2$<br>(10 <sup>-12</sup> erg) | $\phi$<br>(eV)           | $f$<br>(10 <sup>4</sup> dyn cm <sup>-1</sup> ) | $\beta$<br>(10 <sup>-12</sup> dyn <sup>-1</sup> cm <sup>2</sup> ) | $\nu_0$<br>(THz)    | $\theta_D$<br>(K) | $\gamma$           |
| 15           | 0.623                | 1.858                                 | 0.751                   | 2.029                                    | -144.920                 | 12.91  | 3.029   | 9.469               | 454.47            | 2.32               |
| 60           | 0.622                | 1.852                                 | 0.750                   | 2.026                                    | -144.963                 | 12.95  | 3.021   | 9.485               | 455.22            | 2.33               |
| 105          | 0.621                | 1.846                                 | 0.749                   | 2.022                                    | -145.005                 | 12.99  | 3.013   | 9.500               | 455.96            | 2.34               |
| 195          | 0.619                | 1.834                                 | 0.746                   | 2.015                                    | -145.090                 | 13.07  | 2.997   | 9.531               | 457.44            | 2.36               |
| 240          | 0.618                | 1.828                                 | 0.745                   | 2.011                                    | -145.133                 | 13.12  | 2.989   | 9.547               | 458.18            | 2.37               |
| 300          | 0.617                | 1.821                                 | 0.744                   | 2.006                                    | -145.181                 | 13.17  | 2.978   | 9.567               | 459.17            | 2.38               |
| (Expt)       | —                    | —                                     | —                       | —  | (-140.52) <sup>a</sup>   | —  | —   | (8.58) <sup>b</sup> | —                 | (2-3) <sup>c</sup> |

<sup>a</sup> Reference [33]; <sup>b</sup> reference [34]; <sup>c</sup> reference [35].

**Table 3.** Model parameters and thermodynamic properties of Ca<sub>0.85</sub>Sm<sub>0.15</sub>MnO<sub>3</sub>.

| <i>T</i> (K) | Model parameters     |                                       |                         |  | Thermodynamic properties |  |   |                     |                   |                    |
|--------------|----------------------|---------------------------------------|-------------------------|--|--------------------------|--|---|---------------------|-------------------|--------------------|
|              | Mn–O<br>$\rho_1$ (Å) | Mn–O $b_1$<br>(10 <sup>-12</sup> erg) | Ca/Sm–O<br>$\rho_2$ (Å) | Ca/Sm–O $b_2$<br>(10 <sup>-12</sup> erg) | $\phi$<br>(eV)           | $f$<br>(10 <sup>4</sup> dyn cm <sup>-1</sup> ) | $\beta$<br>(10 <sup>-12</sup> dyn <sup>-1</sup> cm <sup>2</sup> ) | $\nu_0$<br>(THz)    | $\theta_D$<br>(K) | $\gamma$           |
| 15           | 0.495                | 1.128                                 | 0.577                   | 1.557                                    | -147.536                 | 14.12  | 3.012   | 9.903               | 475.29            | 2.78               |
| 60           | 0.494                | 1.123                                 | 0.576                   | 1.554                                    | -147.555                 | 14.16  | 3.005   | 9.918               | 476.00            | 2.79               |
| 105          | 0.493                | 1.119                                 | 0.575                   | 1.551                                    | -147.573                 | 14.20  | 2.998   | 9.933               | 476.71            | 2.80               |
| 195          | 0.492                | 1.114                                 | 0.573                   | 1.545                                    | -147.610                 | 14.28  | 2.984   | 9.962               | 478.12            | 2.82               |
| 240          | 0.491                | 1.105                                 | 0.572                   | 1.542                                    | -147.628                 | 14.33  | 2.977   | 9.977               | 478.82            | 2.83               |
| 300          | 0.489                | 1.090                                 | 0.571                   | 1.538                                    | -147.652                 | 14.38  | 2.967   | 9.996               | 479.76            | 2.85               |
| (Expt)       | —                    | —                                     | —                       | —  | (-140.52) <sup>a</sup>   | —  | —   | (8.58) <sup>b</sup> | —                 | (2-3) <sup>c</sup> |

<sup>a</sup> Reference [33]; <sup>b</sup> reference [34]; <sup>c</sup> reference [35].

The specific heat at constant volume ( $C_v$ ) for SmMnO<sub>3</sub>, Sm<sub>0.55</sub>Sr<sub>0.45</sub>MnO<sub>3</sub> and Ca<sub>0.85</sub>Sm<sub>0.15</sub>MnO<sub>3</sub> have been calculated at different temperatures ( $T$ ) using the well known expression [18–20]:

$$C_v = 9R \left( \frac{T}{\theta_D} \right)^3 \int_0^{\frac{\theta_D}{T}} \frac{e^x x^4}{e^x - 1} dx. \quad (7)$$

The specific heat at constant pressure is calculated using [18]:

$$C_p = TV\alpha^2 B_T + C_v, \quad (8)$$

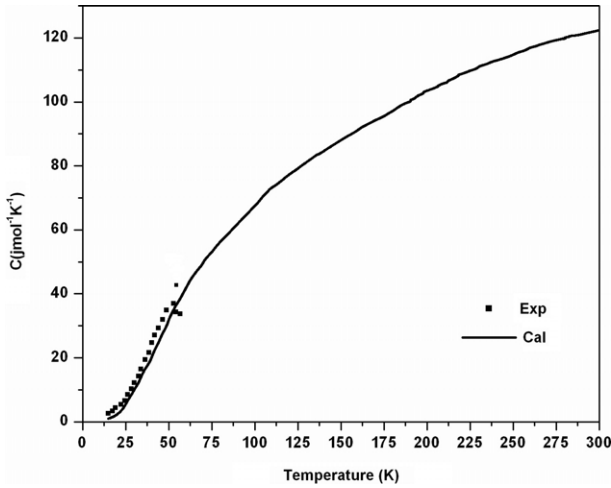
where  $\alpha$  is the linear thermal expansion coefficient,  $B_T$  is the isothermal bulk modulus, and  $V$  is the unit cell volume.

In addition, we have computed the thermodynamic parameters, such as the cohesive energy ( $\phi$ ), molecular force constant ( $f$ ), compressibility ( $\beta$ ), Restrahlen frequency ( $\nu_0$ ), Debye temperature ( $\theta_D$ ) and Grüneisen parameter ( $\gamma$ ) of

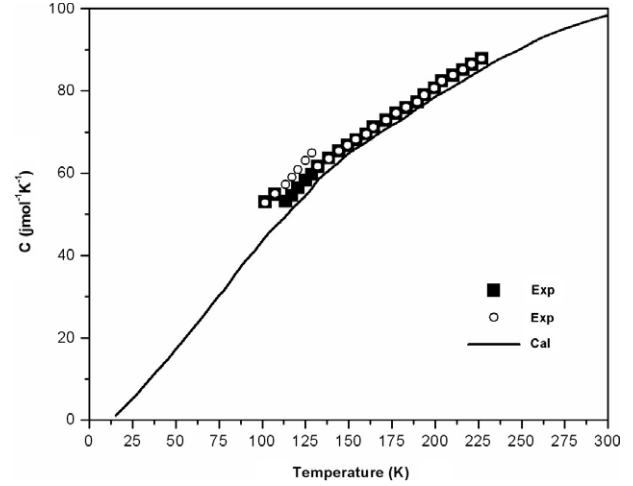
SmMnO<sub>3</sub>, Sm<sub>0.55</sub>Sr<sub>0.45</sub>MnO<sub>3</sub> and Ca<sub>0.85</sub>Sm<sub>0.15</sub>MnO<sub>3</sub> using their expressions reported elsewhere [18, 19]. The computed results thus obtained are presented and discussed below.

### 3. Computed results and discussion

Using the disposable model parameters listed in tables 1–3, the values of  $\phi$ ,  $f$ ,  $\beta$ ,  $\nu_0$ ,  $\theta_D$  and  $\gamma$  are computed and depicted in tables 1, 2 and 3 for SmMnO<sub>3</sub>, Sm<sub>0.55</sub>Sr<sub>0.45</sub>MnO<sub>3</sub> and Ca<sub>0.85</sub>Sm<sub>0.15</sub>MnO<sub>3</sub>, respectively. The chief aim of the application of the present model is to reproduce the observed physical properties such as the transport and thermodynamic properties of perovskite manganites. Keeping this objective in view, we find that our results obtained for most of the transport properties are closer to the experimental data [10, 33–35] available only at 300 K. The cohesive energy is the measure of strength of the force binding the atoms together in solids. This



**Figure 1.** Variation of specific heat with temperature of  $\text{SmMnO}_3$  where the solid line (—) and squares (■) represent the model calculation and experimental [10] values respectively.

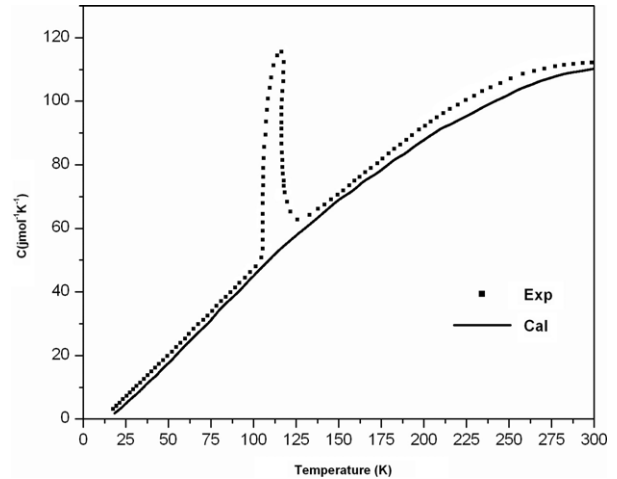


**Figure 2.** Variation of specific heat with temperature of  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  where the solid line (—) and squares (■) and open circles (○) represent the model calculation and experimental [11] values respectively.

fact is exhibited from our cohesive energy results which follow the similar trend of variation with  $T$ , as is revealed by the bulk modulus that represents the resistance to volume change [32]. This feature is indicated from tables 1–3, which show that the values of the cohesive energy ( $\phi$ ) decreases from  $-143.885$  eV for  $\text{SmMnO}_3$  to  $-145.181$  eV for  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  and  $-147.652$  eV for  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  with Sr (Ca) dopings; the same trend of variation is also exhibited by the bulk modulus. Due to a lack of experimental data, we have compared the values of cohesive energy of pure  $\text{SmMnO}_3$  with that of  $\text{LaMnO}_3$  [33], which is a member of the same family. The negative values of cohesive energy show that the stability of these manganites is intact. It is also noticed from tables 1–3 that the values of hardness ( $b_1$ ,  $b_2$ ) and the stability ( $\phi$ ) decrease with temperature.

We have also calculated the values of the molecular force constants ( $f$ ) and Restrahlen frequencies ( $\nu_0$ ) (see tables 1–3) and found that  $\nu_0$  increases with temperature ( $T$ ). Since the Restrahlen frequency is directly proportional to the molecular force constant ( $f$ ) therefore both of them vary with the temperature accordingly for different concentrations ( $x$ ). The values of Restrahlen frequency are almost in the same range as that reported for the parent member  $\text{LaMnO}_3$  ( $\nu_0 = 8.58$  THz) [34]. The calculated value of Debye temperature ( $\theta_D$ ) for  $\text{SmMnO}_3$  (442.822 K) is approximately in agreement with the experimental data (465 K) available only at room temperature [10]. The calculated values of ( $\theta_D$ ) for  $\text{SmMnO}_3$ ,  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  and  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  at 300 K are 442.822, 459.170 and 479.764 K, which lie within the Debye temperature range (300–550 K) often found in perovskite manganites. The Grüneisen parameters ( $\gamma$ ) obtained by us are found to lie between 2 and 3, which are similar to the values observed by Dai *et al* [35].

The specific heat ( $C$ ) values calculated by us for pure  $\text{SmMnO}_3$  at temperatures  $15 \text{ K} \leq T \leq 300 \text{ K}$  are displayed in figure 1 and found to be in good agreement with the measured data [10] at lower temperatures  $15 \text{ K} \leq T \leq 60 \text{ K}$ . Our results have followed a trend more or less similar to those exhibited by



**Figure 3.** Variation of specific heat with temperature of  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  where the solid line (—) and squares (■) represent the model calculation and experimental [12] values respectively.

the experimental curve at lower temperatures. A sharp peak is observed in the experimental specific heat curve at  $\sim 59$  K due to the A-type AF ordering. This feature is not revealed from our calculated results and this might be due to the exclusion of the spin correlation wave contribution in the MRIM. The change in Mn–O distance by the substitution of a Sm site by Sr or Ca increases  $\theta_D$  and hence there is a consistent decrease in the specific heat values corresponding to the doping in both of the cases (see figures 2 and 3). Hence, the concentration ( $x$ ) dependence of  $\theta_D$  in  $\text{SmMnO}_3$ ,  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  and  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  suggests that increased hole doping drives the system effectively towards the strong electron–phonon coupling regime. The present MRIM calculations yield similar specific heat values at low temperatures (below 60 K) where the acoustic phonons play an important role.

On doping Sr ( $x = 0.45$ ) in  $\text{SmMnO}_3$ , the specific heat increases monotonically with temperature as shown in figure 2. The experimental specific heat results [11] for  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  show two critical end points at 128.6 and 113.3 K which might be due to the ferromagnetic to paramagnetic transition. It is also seen from figure 2 that our theoretical results are in closer agreement with the available experimental [11] data in the middle range of temperature  $100 \text{ K} \leq T \leq 225 \text{ K}$ .

In the case of  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$ , there are some special features which deserve detailed discussion. The specific heat also increases with temperature in  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$  as seen from figure 3. The MRIM results have fairly well reproduced the experimental specific heat data in the temperature ranges  $15 \text{ K} \leq T \leq 100 \text{ K}$  and  $120 \text{ K} \leq T \leq 300 \text{ K}$  except for the range  $112 \text{ K} \leq T \leq 120 \text{ K}$ , in which a cusp like anomaly occurs at 115 K in the specific heat curve (see figure 3); this feature corresponds to the phase transition from an orthorhombic  $Pnma$  to a monoclinic  $P2_1/m$  as revealed from the neutron diffraction data [12]. However, the description of this anomaly is beyond the scope of our present model due to the inherent deficiency from not including the ferromagnetic spin wave contribution and Jahn–Teller distortion effect in our calculation.

#### 4. Conclusion

The varied exposition of the temperature-dependent thermodynamical properties of perovskite manganites ( $\text{SmMnO}_3$ ,  $\text{Sm}_{0.55}\text{Sr}_{0.45}\text{MnO}_3$  and  $\text{Ca}_{0.85}\text{Sm}_{0.15}\text{MnO}_3$ ) attained by us is remarkable in view of the inherent simplicity of the modified rigid ion model.

All this indicates the power and usefulness of the MRIM as having the potential to explain a variety of physical properties (such as cohesive, thermal, elastic, thermodynamic) of the pure and doped CMR materials. However, the efforts that have been devoted by many experimental workers to observe magnetic transitions and properties, to the best of our knowledge, only a few groups are involved with the study of temperature- and composition-dependent properties of perovskite manganites (or CMR) materials. On the basis of the overall descriptions, it may be concluded that our modified rigid ion model has reproduced thermodynamic properties that correspond well to the experimental data. The present results can be further improved by incorporating the effects of the ferromagnetic spin wave contribution and Jahn–Teller distortion in the framework of the MRIM in a future research programme.

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